

The Segmented Pay-as-Clear Approach for (Energy) Markets

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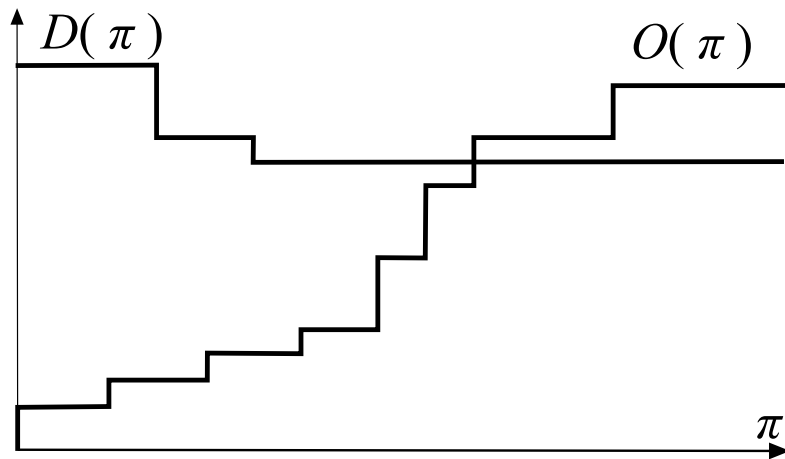
The HEXAGON Workshop on power grids
Bergamo (Italy), June 19, 2024

- 1 A brief introduction to Pay-as-Clear (energy) markets
- 2 The Problem
- 3 Discussing the problem
- 4 Our solution, in details
- 5 Can it work?
- 6 Can it be applied to practical markets?
- 7 Conclusions

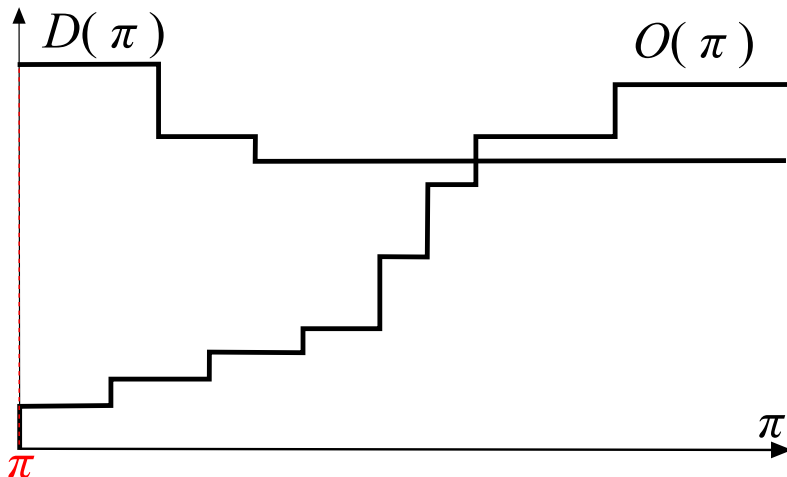
The Pay-as-Clear market clearing mechanism

- Market = sellers + buyers of a fungible divisible commodity (energy)
 - set S of **sell offers** $\langle sp_j, sq_j \rangle$: will sell (\leq) sq_j for a price $\geq sp_j$
 - set B of **purchase bids** $\langle bp_i, bq_i \rangle$: will buy (\leq) bq_i for a price $\leq bp_i$
- **Nondecreasing offer curve** (not function) $O(\pi) = \sum_{j: sp_j \geq \pi} sq_j$
- **Nonincreasing demand curve** (not function) $D(\pi) = \sum_{j: bp_j \leq \pi} bq_j$
- **Clearing price** $\pi^* =$ “where $O(\pi)$ and $D(\pi)$ meet” \implies total amount q^* (of energy) exchanged over the market
- Forget about market failures and degeneracy ...
- But why Pay-as-Clear?

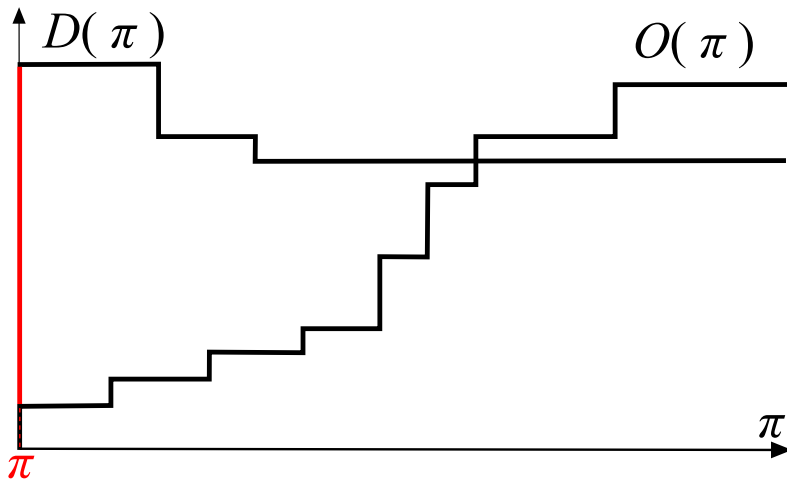
The Pay-as-Clear Model, graphically



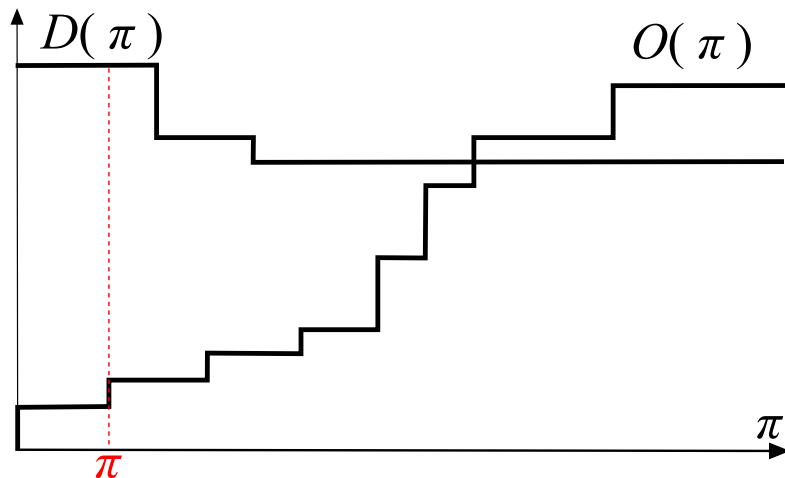
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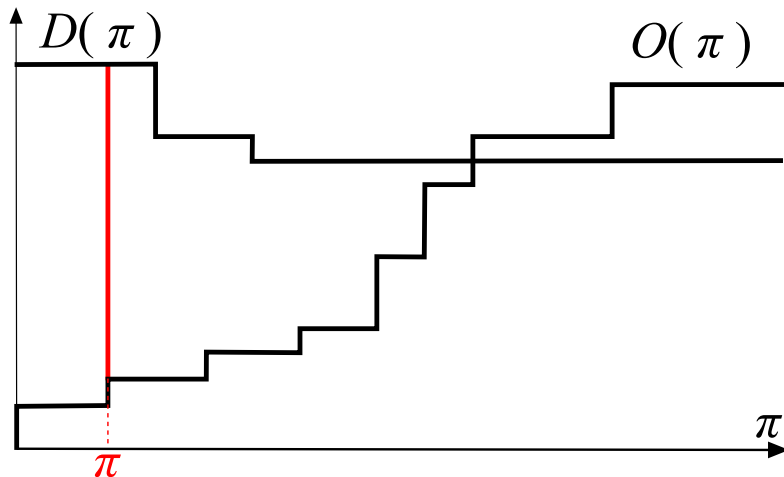
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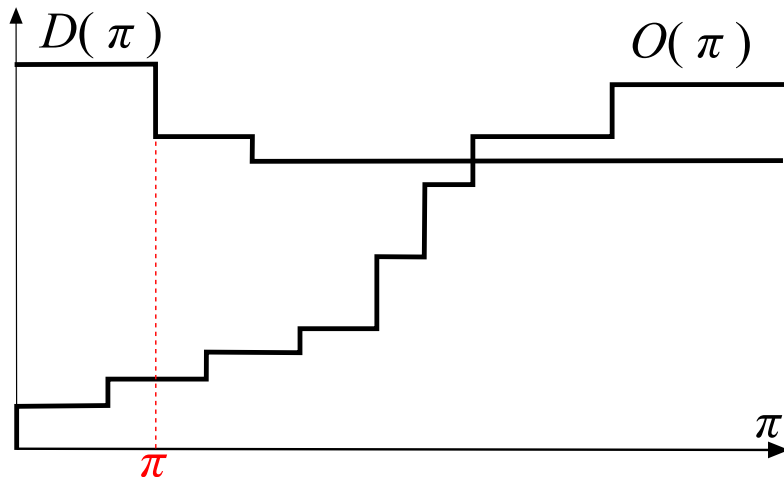
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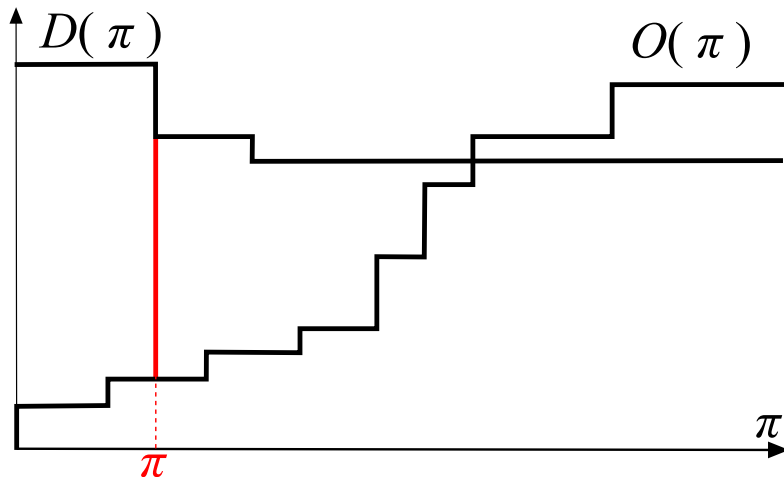
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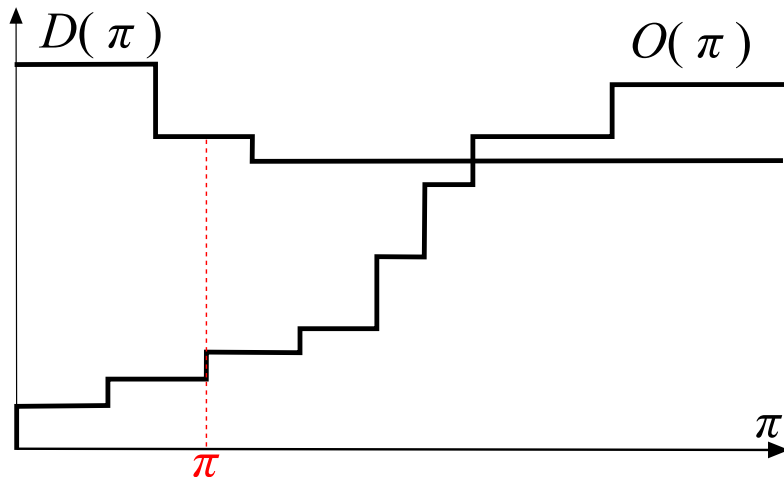
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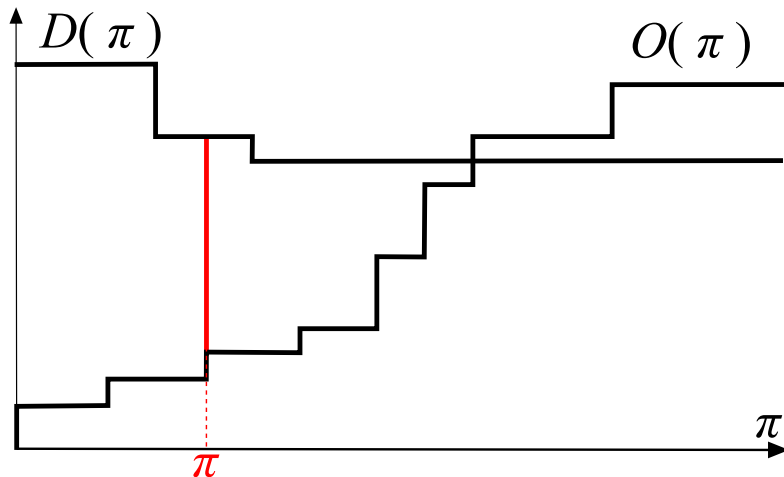
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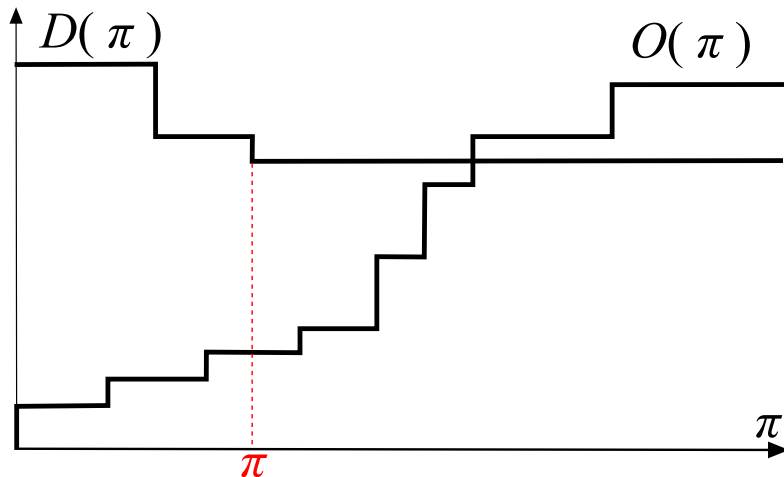
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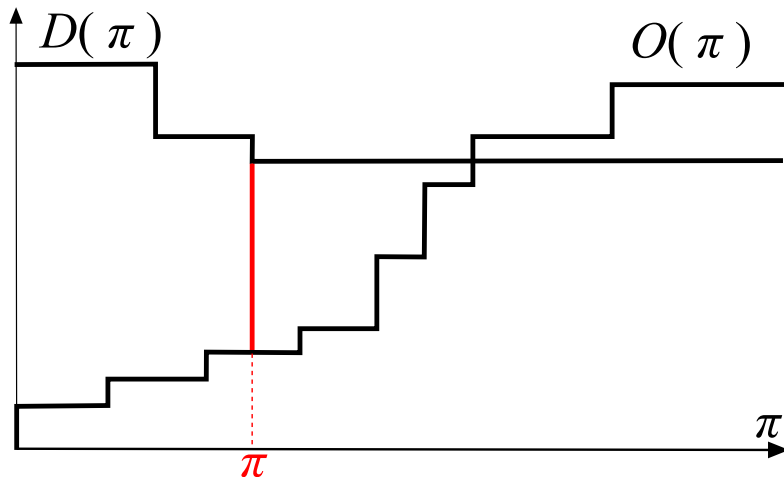
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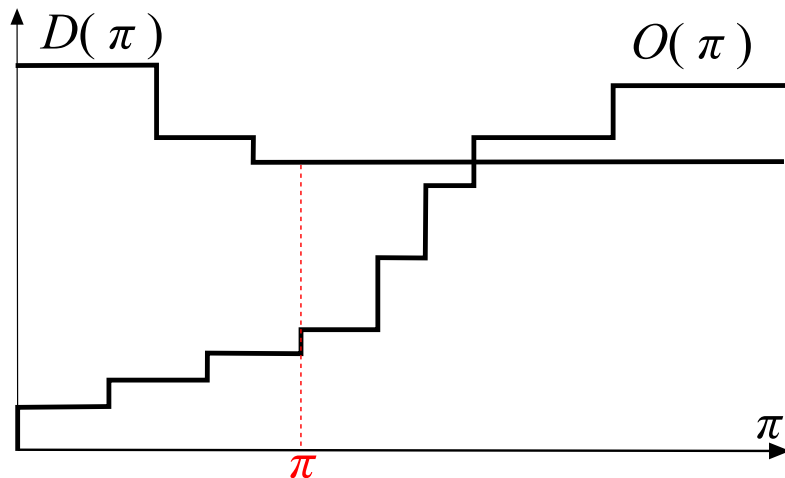
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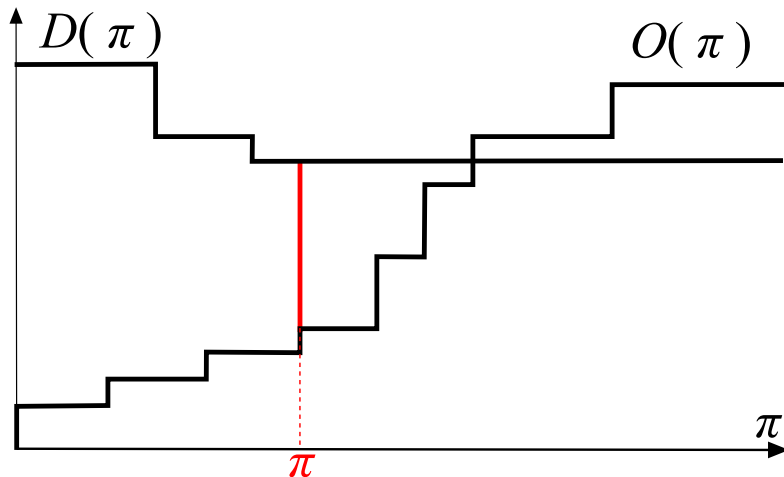
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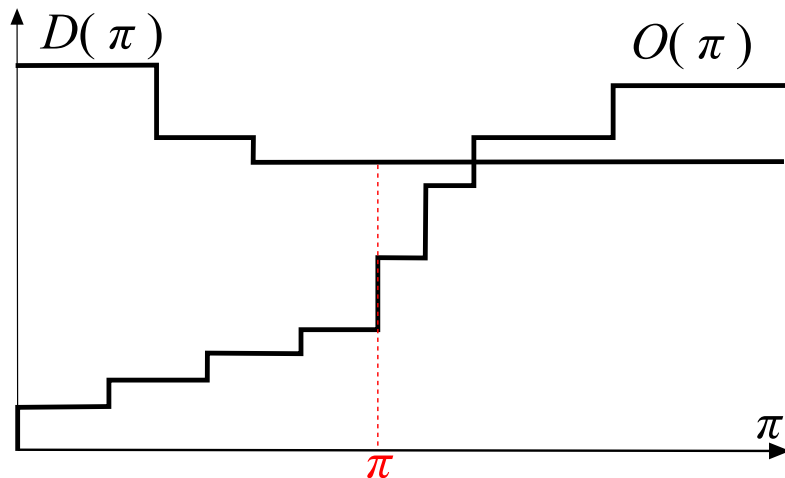
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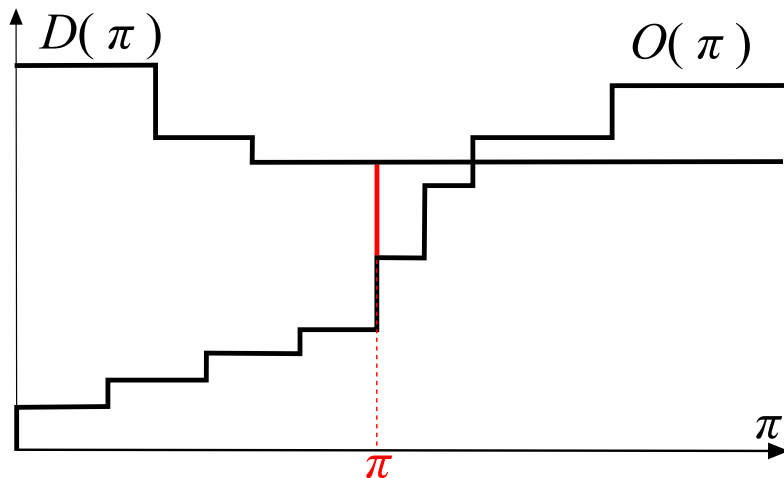
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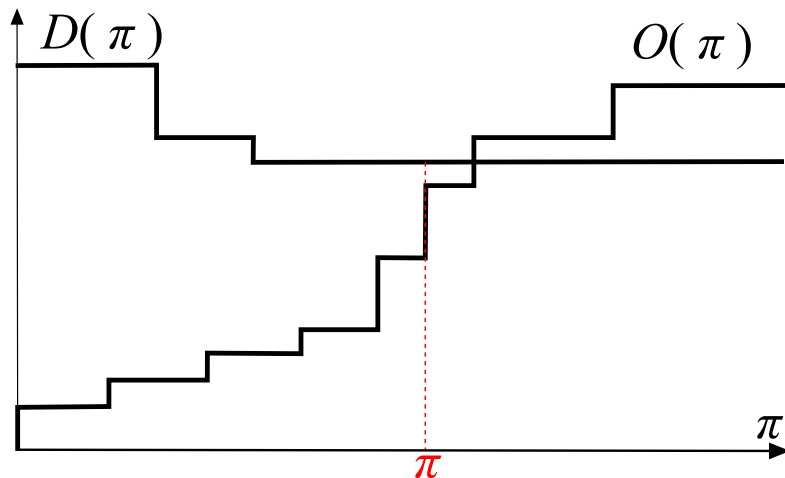
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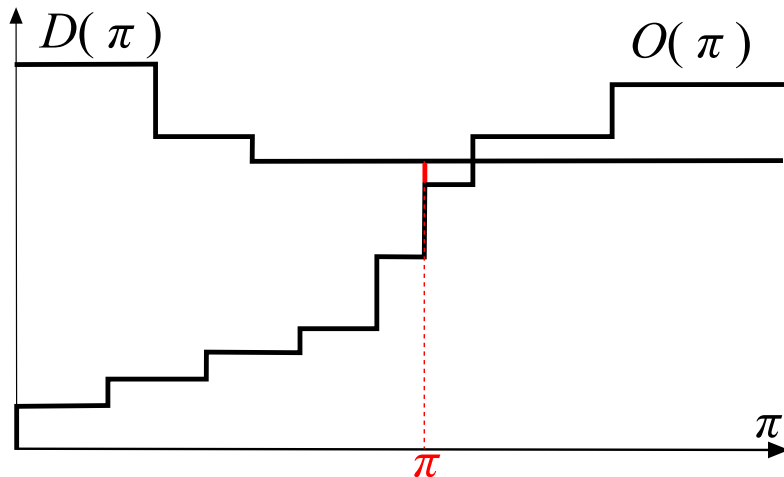
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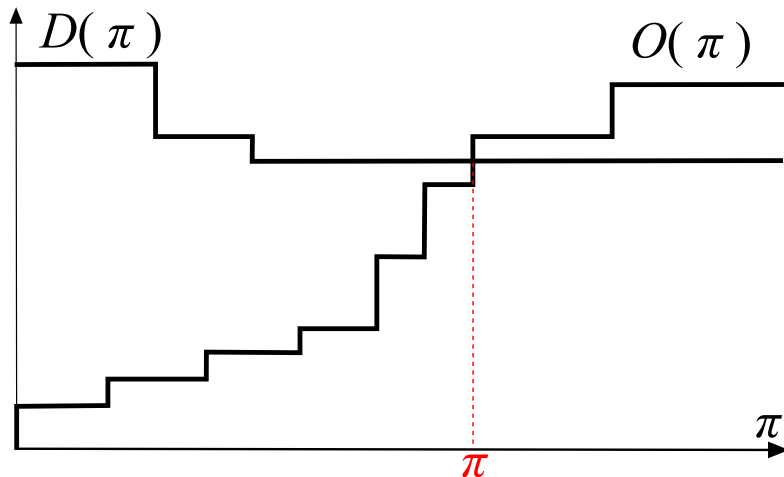
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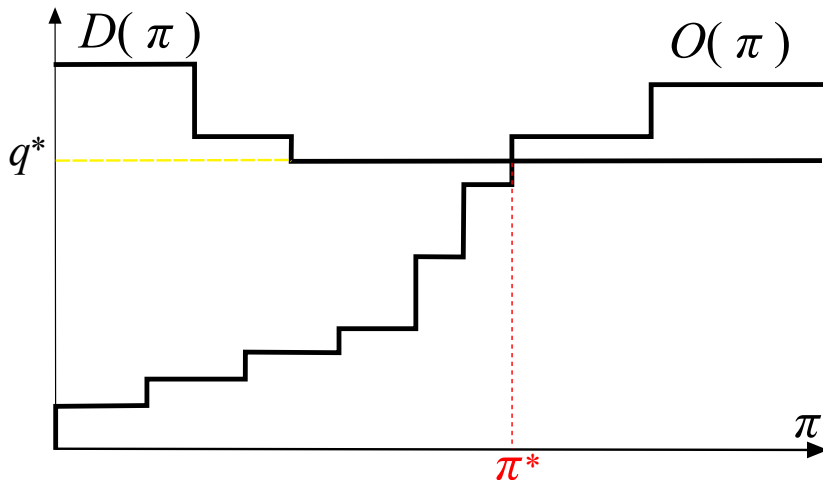
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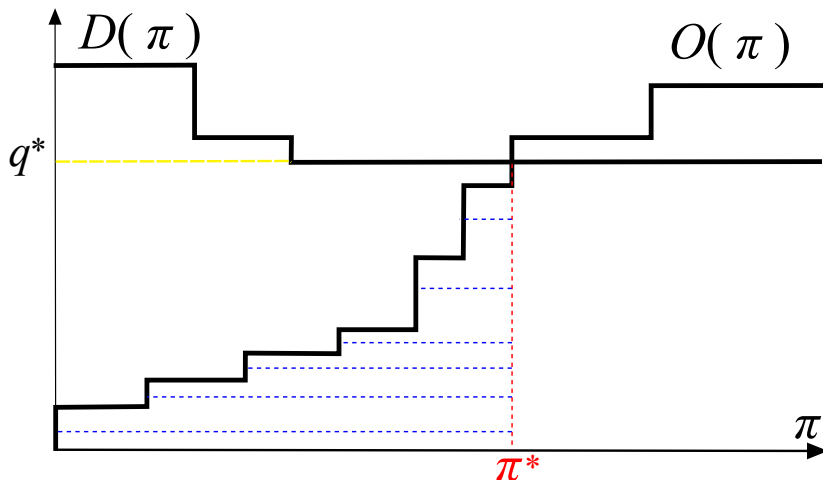
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The Pay-as-Clear Model, graphically

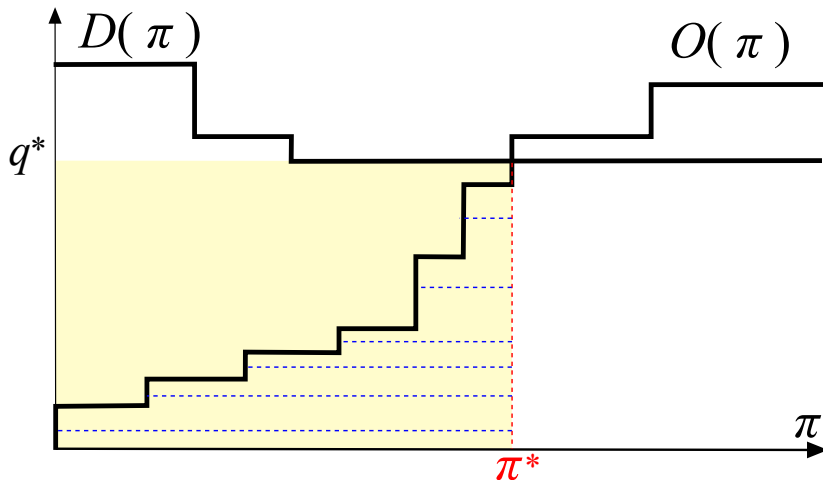


The Pay-as-Clear Model, graphically



- Everyone paid at the clearing price π^*

The Pay-as-Clear Model, graphically



- Everyone paid at the clearing price π^* \implies total system cost = $\pi^* q^*$

Everyone loves it because it's an LP

- Let's simplify: **fixed demand** \equiv **only sell offers** (\approx true in electricity)

- Primal / dual **market clearing problems**:

$$\min \sum_{j \in S} sp_j s_j \quad (1) \quad \max \sum_{j \in S} sq_j \eta_j + \pi d \quad (4)$$

$$0 \leq s_j \leq sq_j \quad j \in S \quad (2) \quad \eta_j + \pi \leq sp_j, \eta_j \leq 0 \quad j \in S \quad (5)$$

$$\sum_{j \in S} s_j = d \quad (3)$$

- Primal feasibility + dual feasibility + **complementary slackness**

$$\eta_j (s_j - sq_j) = 0 \quad j \in S \quad (6)$$

$$(sp_j - \eta_j - \pi) s_j = 0 \quad j \in S \quad (7)$$

\implies **optimal** π^* **the market clearing price**

- Easy to see with just a bit of logic, but I like it different

I love it even more because it's a Lagrangian

- **Lagrangian relaxation** of (1)–(3) w.r.t. (3) (multiplier π):

$$\min \sum_{j \in S} sp_j s_j + \pi(d - \sum_{j \in S} s_j) = \pi d + \sum_{j \in S} (sp_j - \pi) s_j \quad (8)$$

$$0 \leq s_j \leq sq_j \quad j \in S \quad (2)$$

clearly separable in j , (3) only **linking constraint**

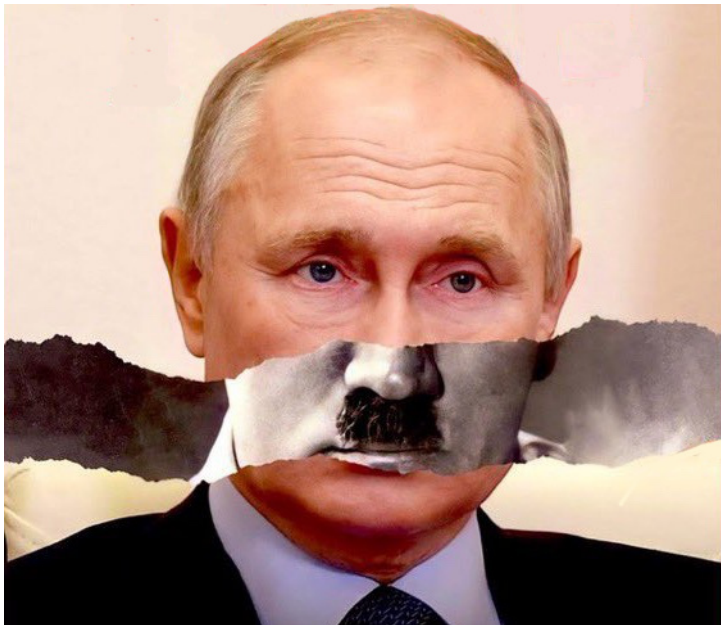
- $\pi > sp_j \implies sp_j - \pi < 0 \implies s_j^*(\pi) = sq_j$, i.e.,
as soon as the price is $>$ than my asking price I sell everything
- $\phi(\pi)$ dual function, $g(\pi) = d - \sum_{j \in S} s_j^*(\pi)$ its (sub)gradient
- π^* optimal $\iff g(\pi^*) = 0 \iff \sum_{j \in S} s_j^*(\pi) = d$
- Adjust s_j^* for which $sp_j = \pi^*$ to make it work (nondifferentiable)
- Not too important, just faster than juggling complementary slackness

It has many nice properties

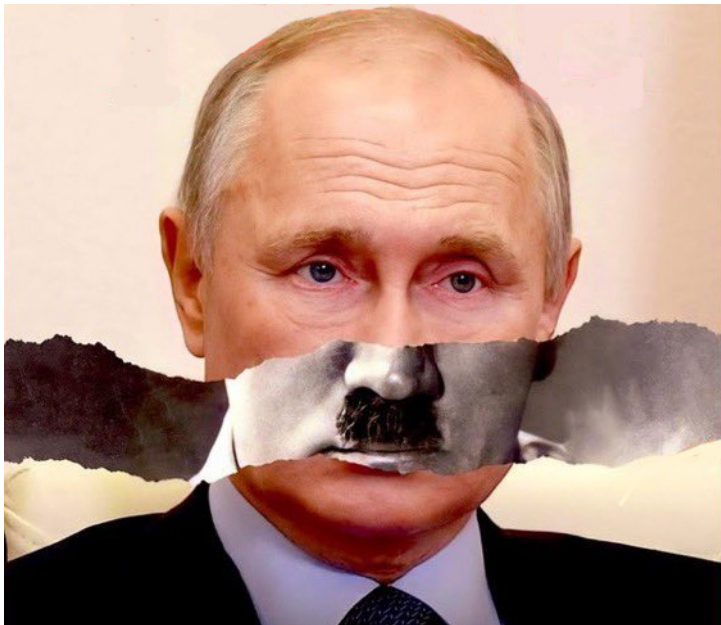
- Day-Ahead Market solved every day for every hour of the next day (plus primary/secondary reserve markets, ancillary services, ...)
- Long-term average gives long-term price signal: how much is worth investing in new generation (5+y to build, 10+y amortization, ...)
- Hourly price gives short-term price signal: how much energy is worth in this specific hour, crucial for Unit Commitment (peak shaving ...)
- Pay-as-bid (apparently) not as good (don't ask ...)
- Can resist complications: variable demand, (DC) network constraints, strange market constructs (unique national price, complex bids, ...) because it's an LP or MPCC $\equiv \mathcal{NP}$ -hard, but we are happy with that
- Everyone's happy then, so what's the problem?

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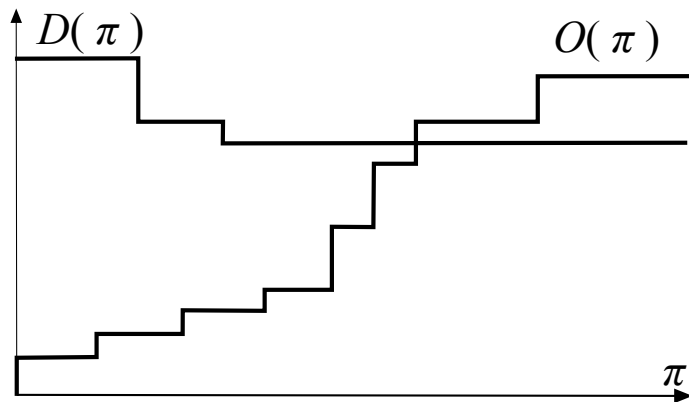
The Problem



The Problem – Root Cause

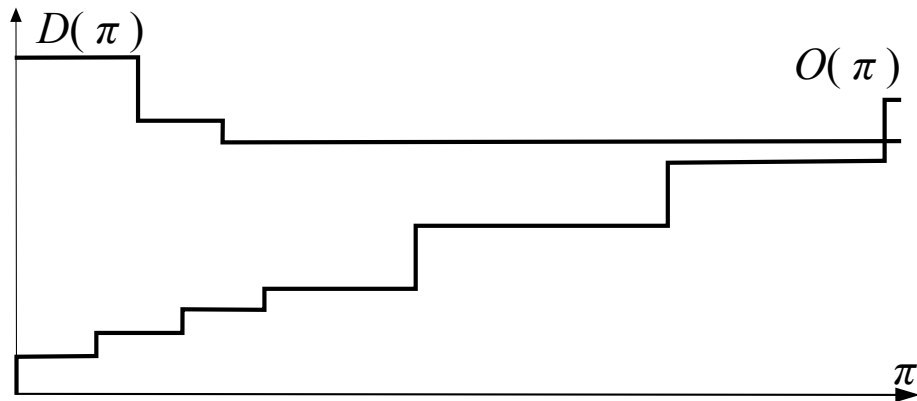


The Problem – Technical – graphically



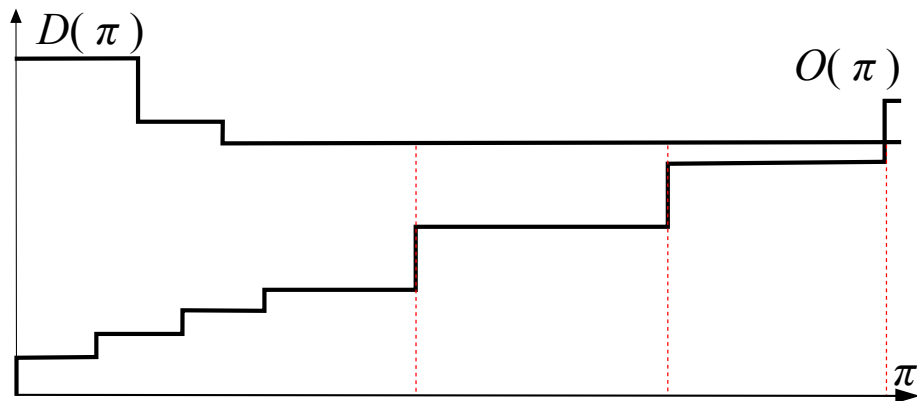
- W.r.t. “normal” times

The Problem – Technical – graphically



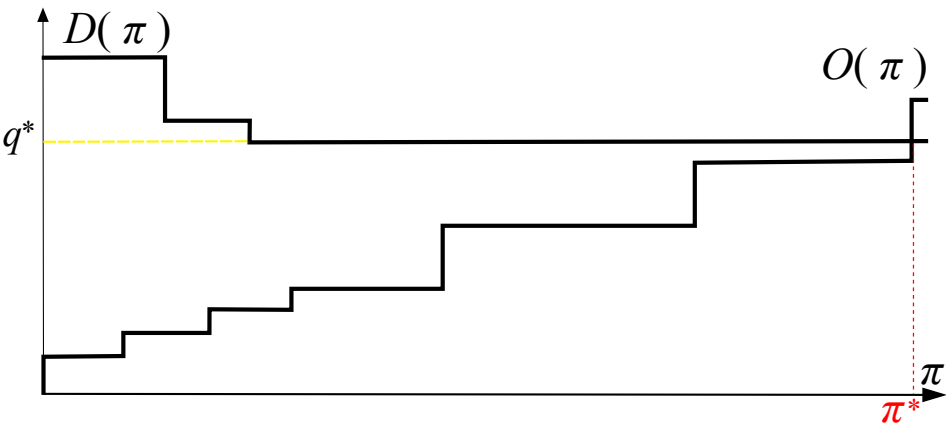
- W.r.t. “normal” times gas prices shot up

The Problem – Technical – graphically



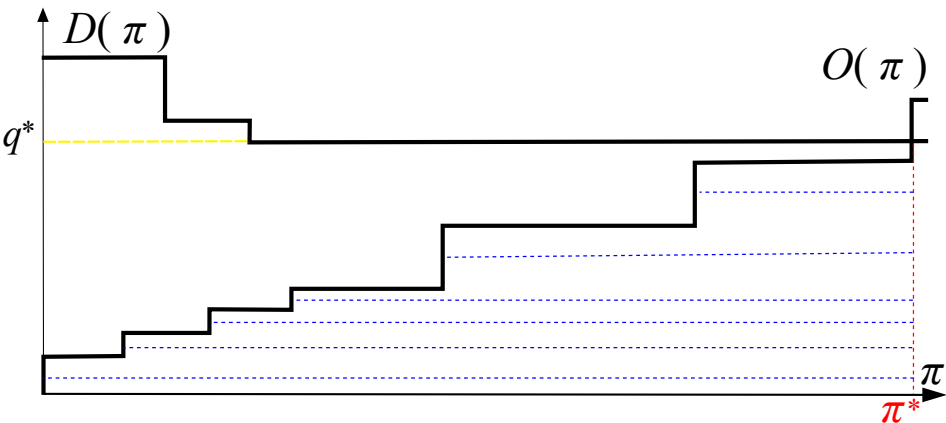
- W.r.t. “normal” times gas prices shot up \implies gas-fired units increased sp_j

The Problem – Technical – graphically



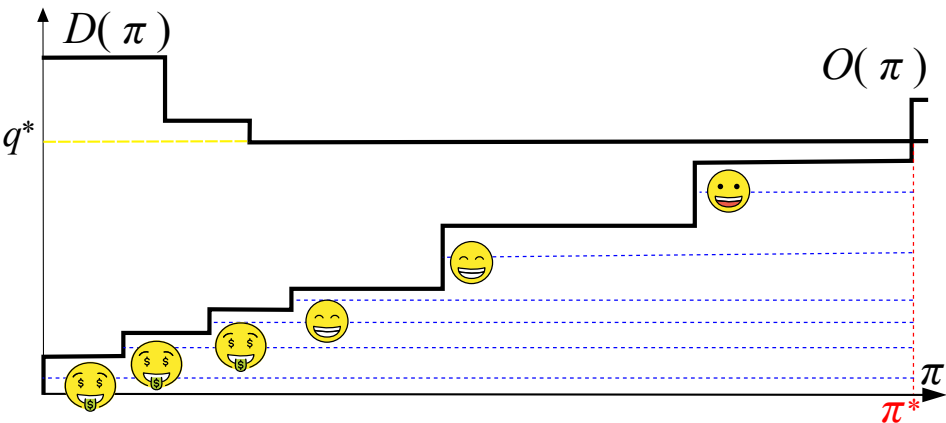
- W.r.t. “normal” times **gas prices shot up** \implies gas-fired units **increased sp_j**
- **π^* shot up,**

The Problem – Technical – graphically



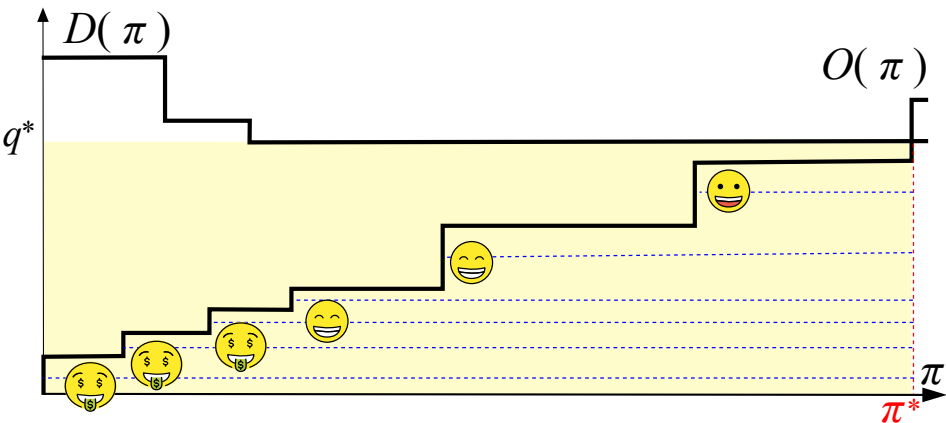
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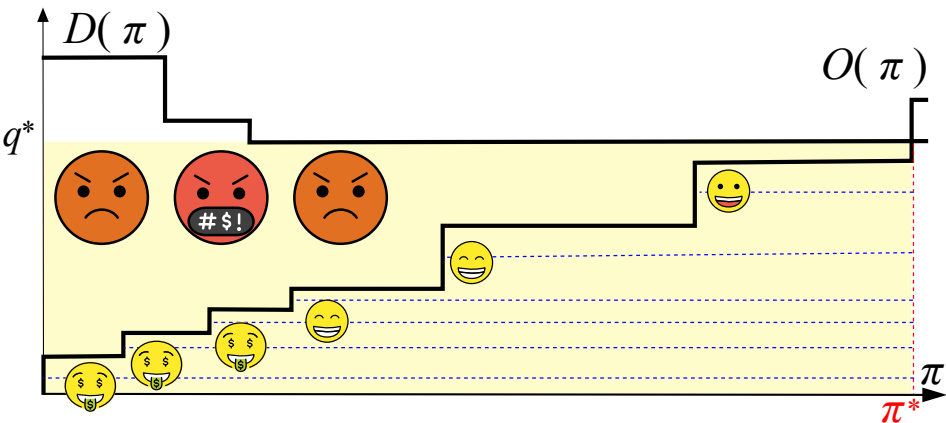
- W.r.t. “normal” times gas prices shot up \implies gas-fired units increased sp_j
- π^* shot up, producers corked spumante,

The Problem – Technical – graphically



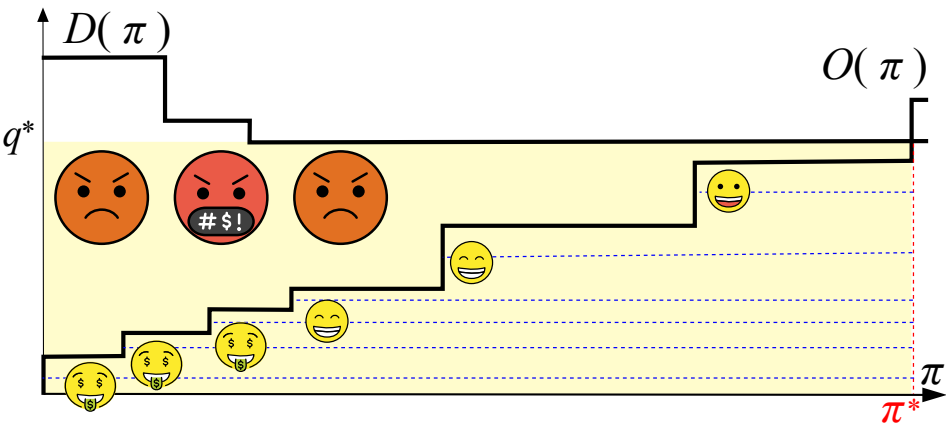
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The Problem – Technical – graphically



- W.r.t. “normal” times gas prices shot up \implies gas-fired units increased sp_j
- π^* shot up, producers corked spumante, consumers went down in flames

The Problem – Technical – graphically



- W.r.t. “normal” times gas prices shot up \implies gas-fired units increased sp_j
- π^* shot up, producers corked spumante, consumers went down in flames
- The real energy cost had increased way less than the clearing price

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Us discussing energy problems goes a loooooong way



(Pc) h^* is conv. \exists ^{data} ϵ continuous P^* such that $h^* \in H^{\epsilon, \epsilon, \epsilon, \epsilon, \epsilon}$ $\forall \epsilon > 0$ $\forall \epsilon > 0$

(Pd) $h^* \in H^{\epsilon, \epsilon, \epsilon, \epsilon, \epsilon}$ $\forall \epsilon > 0$

$$(Dd) \equiv (Pb) \quad (dz^* = dx^*)^{-1}$$

$$(Dc) \equiv (Pa) \quad [0, z^*] \cap \mathcal{C} \cap \mathcal{R} \neq \emptyset$$

$$h^*(z) = \delta_{\mathcal{C}}(z) - 1$$



$$(P_k = [0, x^*], \dots, x^*] \rightarrow k^* \text{ is bounded}$$

$\delta_{\text{cont}} P_k^*$ P_k^* is bounded

$$\neq \exists \Delta$$

What Fabrizio wanted

- Partition $S = S^r \cup S^g$:
 $S^r =$ reserved (renewables) market,
 $S^g =$ general (gas-fired) market
- Have producers in each market only slog it out among themselves
 \implies different prices for the same commodity, reflecting fundamentally different cost structure of sets of producers
- Both markets must satisfy the same demand
- Economists were sharpening forks and lighting up pyres, but that was not what was bothering me
- How can you have two markets be separate, and then “magically” agree on the demand each will satisfy?
- Never believed in magic, and never were afraid to tell
- Some wishes just never come true, I’m not the fairy godmother!

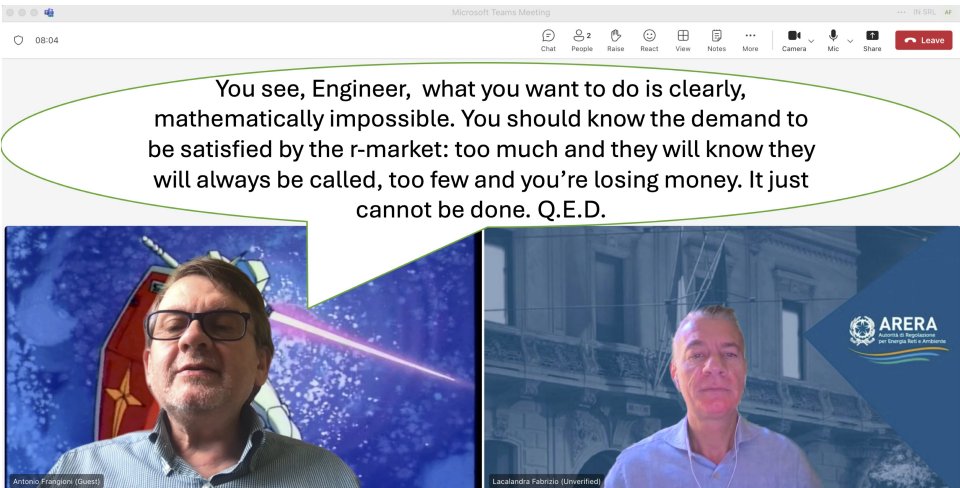
How the discussion went

Microsoft Teams Meeting

08:04

Chat People Raise React View Notes More Camera Mic Share Leave

You see, Engineer, what you want to do is clearly, mathematically impossible. You should know the demand to be satisfied by the r-market: too much and they will know they will always be called, too few and you're losing money. It just cannot be done. Q.E.D.



Antonio Frangioni (Guest)

Lacialandra Fabrizio (Unverified)

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How the discussion went

Microsoft Teams Meeting

08:41

Chat People Raise React View Notes More Camera Mic Share Leave

But we can make the demand of the r-market
a variable of the problem, can't we?

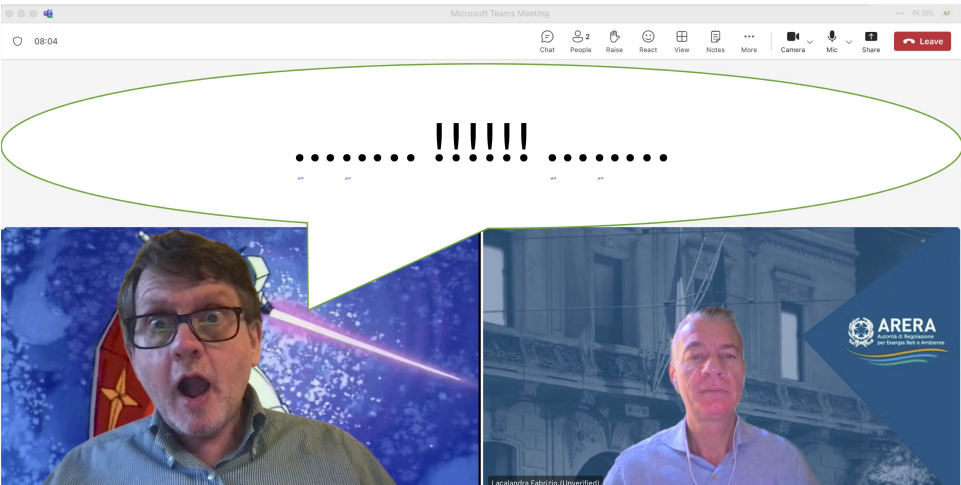
Antonio Frangioni (Guest)

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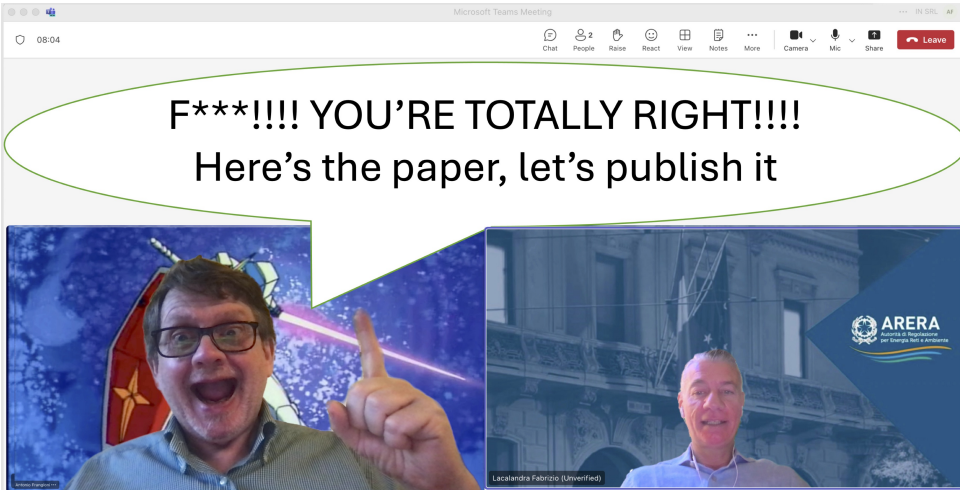
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The screenshot shows a Microsoft Teams meeting interface. At the top, the title bar reads "Microsoft Teams Meeting" and the time is "08:41". A toolbar contains icons for Chat, People, Raise, React, View, Notes, More, Camera, Mic, Share, and a red "Leave" button. The main content area displays a slide with a green speech bubble containing the text: "But we can make the demand of the r-market a variable of the problem, can't we?". Below the slide are two video thumbnails. The left thumbnail shows Antonio Frangioni (Guest) with a space-themed background. The right thumbnail shows Lacalandra Fabrizio (Unverified) with an ARERA logo in the background.

How the discussion went



How the discussion went



The image shows a screenshot of a Microsoft Teams meeting interface. At the top, the title bar reads "Microsoft Teams Meeting" and "IN SRL AF". The meeting time is "08:04". The top navigation bar includes icons for Chat, People (2), Raise, React, View, Notes, More, Camera, Mic, Share, and a red "Leave" button. A large green speech bubble contains the text: "F***!!!! YOU'RE TOTALLY RIGHT!!!! Here's the paper, let's publish it". Below the speech bubble are two video thumbnails. The left thumbnail shows a man with glasses and a blue shirt pointing upwards, with a background of a red and white flag and a blue sky with a white plane. The right thumbnail shows a man in a blue shirt in front of a building, with the ARERA logo (Autorità di Regolazione per Energia Reti e Ambiente) in the top right corner. The name "Lacalandra Fabrizio (Unverified)" is visible at the bottom of the right thumbnail.

Microsoft Teams Meeting

08:04

Chat People 2 Raise React View Notes More Camera Mic Share Leave

F*!!!! YOU'RE TOTALLY RIGHT!!!!**
Here's the paper, let's publish it

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Lacalandra Fabrizio (Unverified)

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Segmented-Pay-as-Clear, version I: bilevel program

$$\begin{aligned} \min_{d^r, d^g} \quad & \pi^r d^r + \pi^g d^g \\ & d^r + d^g = d, \quad d^r \geq 0, \quad d^g \geq 0 \\ \pi^r \in \quad & \left\{ \begin{array}{l} \arg \max_{\pi^r, \eta} \quad \sum_{j \in S^r} s q_j \eta_j + \pi^r d^r \\ \eta_j + \pi^r \leq s p_j, \quad \eta_j \leq 0 \quad j \in S^r \end{array} \right. \\ \pi^g \in \quad & \left\{ \begin{array}{l} \arg \max_{\pi^g, \eta} \quad \sum_{j \in S^g} s q_j \eta_j + \pi^g d^g \\ \eta_j + \pi^g \leq s p_j, \quad \eta_j \leq 0 \quad j \in S^g \end{array} \right. \end{aligned}$$

- The two markets compete among them for the demand
- Producers in each market compete among them as usual but **not directly** with producers in the other market
- The **objective is bilinear** (nonconvex), but bilevels are hard anyway: throw it to Gurobi via `BilevelJump`, it'll eat it
- Cannot do worse than PaC (will be obvious shortly)

Segmented-Pay-as-Clear, version II: MPCC

$$\min \pi^r d^r + \pi^g d^g \quad (9)$$

$$d^r + d^g = d \quad , \quad d^r \geq 0 \quad , \quad d^g \geq 0 \quad (10)$$

$$0 \leq s_j \leq sq_j \quad j \in S \quad (2)$$

$$\sum_{j \in S^r} s_j = d^r \quad (11)$$

$$\eta_j + \pi^r \leq sp_j \quad , \quad \eta_j \leq 0 \quad j \in S^r \quad (12)$$

$$\sum_{j \in S^g} s_j = d^g \quad (13)$$

$$\eta_j + \pi^g \leq sp_j \quad , \quad \eta_j \leq 0 \quad j \in S^g \quad (14)$$

$$\eta_j (s_j - sq_j) = 0 \quad j \in S \quad (15)$$

$$(sp_j - \eta_j - \pi^r) s_j = 0 \quad j \in S^r \quad (16)$$

$$(sp_j - \eta_j - \pi^g) s_j = 0 \quad j \in S^g \quad (17)$$

- **Bilinear** objective (9) and complementarity constraints (15)–(17)
- But **one bilinearity can kill the other**

Hocus Pocus, nonlinearity vanish! Thanks Medhi Madani

- Actually, a well-known trick in this line of business
- Multiply (30) by π^r to get

$$\pi^r \sum_{j \in S^r} s_j = \pi^r d^r$$

- Sum (16) over $j \in S^r$ and rearrange:

$$\sum_{j \in S^r} (sp_j - \eta_j) s_j = \pi^r \sum_{j \in S^r} s_j = \pi^r d^r$$

- Now (15) gives $\eta_j s_j = \eta_j s q_j$, thus

$$\pi^r d^r = \sum_{j \in S^r} (sp_j s_j - \eta_j s q_j) \quad (18)$$

- Repeat the arguments for $j \in S^g$ and π^g to get

$$\pi^r d^r + \pi^g d^g = \sum_{j \in S} (sp_j s_j - \eta_j s q_j) \quad (19)$$

- One nonlinearity has vanished in thin air

Segmented Prices-as-Clear, the Final Reformulation

- Only one market, but with a limit on the energy from S^r :

$$\min \sum_{j \in S} sp_j s_j \quad (1) \quad \max \sum_{j \in S} sq_j \eta_j + \pi d + \pi^r d^r \quad (21)$$

$$0 \leq s_j \leq sq_j \quad j \in S \quad (2) \quad \eta_j + \pi \leq sp_j \quad j \in S^g \quad (22)$$

$$\sum_{j \in S^r} s_j \leq d^r \quad (20) \quad \eta_j + \pi + \pi^r \leq sp_j \quad j \in S^r \quad (23)$$

$$\sum_{j \in S} s_j = d \quad (3) \quad \eta_j \leq 0 \quad j \in S \quad (24)$$

$$\pi^r \leq 0 \quad (25)$$

- g-market clears at π , r-market clears at $\pi + \pi^r < \pi$ (cf. (25)) \implies
cannot be worse than PaC, equal if d^r "too large" $\implies \pi^r = 0 \implies$
 $(\pi + \pi^r) \sum_{j \in S^r} s_j + \pi(d - \sum_{j \in S^r} s_j) = \pi d + \pi^r \sum_{j \in S^r} s_j = \pi d + \pi^r d^r$

- Compact reformulation of SPaC, can be linearised using (18):

$$\min \{ \pi d + \pi^r d^r : (\pi, \pi^r) \in \operatorname{argmax} \{ (21)-(25) \} \}$$

- Easy to write as MPCC using (1)–(25) + their complementary slackness

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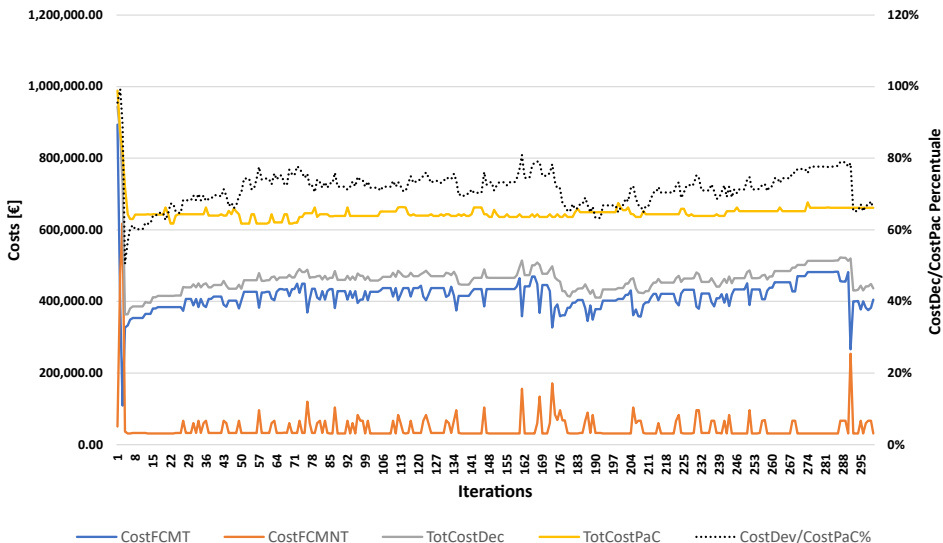
Can it be gamed?

- Of course it can: everyone offers the same (collusion)
- Bad case: all bids on g-market same as PaC, all on the r-market $\pi^* - \varepsilon$
 $\implies \pi^g = \pi^*$, $\pi^r = -\varepsilon \equiv$ negligible decrease of total system cost
- However, this reeks of collusion three miles off
- A result is proven in the paper that roughly speaking says:
if enough bids in the r-market are “fair” then
strategic bidders in the r-market can only achieve a fraction of π^* -PaC
that decreases as $d^r \rightarrow d$ (the size of the r-market increase)
- Complicated, but: if $d^r = 0.8d +$ enough bids in S^r “low”, then
cost on r-market $\leq 33\%$ of π^* -PaC \equiv large decrease of system cost
- Many ifs and buts, but it does seem to indicate:
you need a rather serious collusion to neuter the effect

Would it work in practice?

- **Hard to say**, can try to get clues by **Agent-Based simulations**
- Simple rules to emulate behaviour of (not-too-smart) rational players:
 - if my offer was only partly accepted I very likely stay put
 - if my offer was totally accepted I may (not too likely) increase it
 - if my offer was rejected I will likely decrease it
 - if my offer is rejected for k consecutive rounds I will surely decrease it
 - anyway I will never offer below my baseline (CAPEX + OPEX) realistic cost (wind, solar, ROR hydro, hydro, coal, CGT, gas turbines, ...)
- Tested with demand a varying fraction of d^{\max} (high/low demand hours)
- Lots of parameters, set with common sense (Fabrizio knows) + minimal tuning (don't want to be cherry-picking your agents)
- Not a proof by all means, but an accepted way to get some clues

AB simulations results I



- System costs for the 30-agents test case with $d = 60\%d^{\max}$

AB simulations results II

d / d^{\max}	40%	45%	50%	55%	60%	65%	70%	75%	80%	85%
π^r	73.29	85.12	96.53	97.19	100.09	100.77	104.77	106.16	111.06	110.69
π^g	122.57	123.43	132.05	139.85	145	147.66	150.83	153.19	158.14	164.31
π^{PaC}	74.74	122.22	131.67	139.47	144.79	147.43	150.7	152.98	157.79	164.02
$C(S^r)/C(S^g)$	97.487	31.25	6.044	3.01	2.03	1.508	1.238	1.026	0.899	0.753
TC_SPaC/TC_PaC	98.36%	70.24%	76.19%	75.40%	76.99%	78.26%	80.48%	81.74%	83.44%	82.88%
Min	74.0%	66.4%	71.0%	70.8%	72.7%	74.9%	77.0%	78.2%	79.0%	78.2%
Max	101.5%	100.7%	99.7%	99.3%	98.7%	99.6%	100.4%	100.0%	99.1%	100.3%
Std	3.7%	3.3%	2.7%	2.7%	2.6%	2.3%	2.9%	2.9%	2.9%	3.3%

- Sample results with 100 agents (other similar except with 6, too few)
- Variable d / d^{\max} simulates demand fluctuation over day
- Short-term price signal still there (\implies long-term one)
- Consistent reduction in total cost save for very low demand
- Quite stable results (low std)

AB simulations results takeaways

- System does reach some sort of (realistic?) equilibrium
- Agents correctly learn how to exploit different demand scenarios
- Long- and short-term price signals on π^g conserved (\approx PaC)
- S^r producers still more than decently retributed (realistic prices), just not as much as S^g producers (makes sense)
- **Significant** total system cost reductions (wish I could have 0.001% ...), yet **not unrealistic** one (historical bids gives $> 80\%$, had tell a referee)
- All in all, surprisingly (too?) reasonable results

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Case of elastic demand

$$\min \pi \sum_{i \in B} b_i - \pi^r d^r \quad (26)$$

$$0 \leq s_j \leq sq_j \quad j \in S \quad (27)$$

$$0 \leq b_i \leq bq_i \quad i \in B \quad (28)$$

$$\sum_{j \in S} s_j = \sum_{i \in B} b_i \quad (29)$$

$$\sum_{j \in S^r} s_j \leq d^r \leq \sum_{i \in B} sq_i \quad (30)$$

$$\mu_i + \pi \geq bp_i \quad , \quad \mu_i \geq 0 \quad i \in B \quad (31)$$

$$\eta_j + \pi^r - \pi \geq -sp_j \quad , \quad \eta_j \geq 0 \quad j \in S^r \quad (32)$$

$$\eta_j - \pi \geq -sp_j \quad , \quad \eta_j \geq 0 \quad j \in S^g \quad (33)$$

$$\sum_{i \in B} (bp_i b_i - \mu_i bq_i) \geq \sum_{j \in S} (\eta_j sq_j + sp_j s_j) \quad (34)$$

$$\pi^r (d^r - \sum_{j \in S^r} s_j) = 0 \quad , \quad \pi^r \geq 0 \quad (35)$$

$$\eta_j (sq_j - s_j) = 0 \quad j \in S \quad (36)$$

$$\mu_i (bq_i - b_i) = 0 \quad i \in B \quad (37)$$

$$(\eta_j + \pi^r - \pi + sp_j) s_j = 0 \quad j \in S^r \quad (38)$$

$$(\eta_j - \pi + sp_j) s_j = 0 \quad j \in S^g \quad (39)$$

Important note: economic equilibrium of the system

- Objective (26) can be linearised via (18)
- Same linearization trick: (40) gives $\pi b_i = (bp_i - \mu_i)b_i$,
(37) gives $\mu_i bq_i = \mu_i b_i \implies \pi b_i = bp_i b_i - \mu_i bq_i$
- Of course, same for selling bids (both in S^r and in S^g)
- Thus (linear) **economic equilibrium constraint** (34) ensures **buyers are paying no less than sellers are getting** (enough money around)
- Difference can be positive, have to be given back to buyers as a **discount on their bills** \implies **actual energy price < clearing price π^***
- Weird: some $i \in B$ not accepted even if the **actual energy price < bp_i** , to be well thought-of from the regulatory viewpoint (if ever ...)

Case of elastic demand and (DC) network constraints

$$\min \pi \sum_{i \in B} b_i - \pi^r d^r \quad (26)$$

$$(27), (30), (28), (29), (31), (35), (36), (37), (40) \quad (42)$$

$$m_l \leq \sum_{k \in \mathcal{K}} S_l^k (\sum_{i \in I(k)} b_i - \sum_{j \in J(k)} s_j) \leq M_l \quad l \in \mathcal{L} \quad (43)$$

$$\pi^k = \pi + \sum_{l \in \mathcal{L}} S_l^k (\lambda_l^+ - \lambda_l^-) \quad k \in \mathcal{K} \quad (44)$$

$$\eta_j + \pi^r - \pi^{k(j)} \geq -s p_j, \quad \eta_j \geq 0 \quad j \in S^r \quad (45)$$

$$\eta_j - \pi^{k(j)} \geq -s p_j, \quad \eta_j \geq 0 \quad j \in S^g \quad (46)$$

$$\sum_{i \in B} (b p_i b_i - \mu_i b q_i) - \sum_{j \in S} (\eta_j s q_j + s p_j s_j) \geq \sum_{l \in \mathcal{L}} (M_l \lambda_l^+ - m_l \lambda_l^-) \quad (47)$$

$$(\eta_j + \pi^r - \pi^{k(j)} + s p_j) s_j = 0 \quad j \in S^r \quad (48)$$

$$(\eta_j - \pi^{k(j)} + s p_j) s_j = 0 \quad j \in S^g \quad (49)$$

$$\lambda_l^- (\sum_{k \in \mathcal{K}} S_l^k (\sum_{i \in I(k)} b_i - \sum_{j \in J(k)} s_j) - m_l) = 0 \quad l \in \mathcal{L} \quad (50)$$

$$\lambda_l^+ (M_l - \sum_{k \in \mathcal{K}} S_l^k (\sum_{i \in I(k)} b_i - \sum_{j \in J(k)} s_j)) = 0 \quad l \in \mathcal{L} \quad (51)$$

$$\lambda_l^+ \geq 0, \quad \lambda_l^- \geq 0 \quad l \in \mathcal{L} \quad (52)$$

Adding the Italian Prezzo Unico Nazionale (PUN)

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Adding the Italian Prezzo Unico Nazionale (PUN intended)

- No, you don't really want to see it, just boring (check the paper)
- Take away: if you can do it with PaC, you can do it with SPaC
- MPCC is “lingua franca” of market models, SPaC very natural in MPCC: just add the bound constraint on S^r and the corresponding dual variable
- A few not-entirely-trivial issues (economic equilibrium), but very doable
- Almost obvious multiple segmentation of seller market: just add multiple copies of the constraint and of the dual variable
- Multiple segmentation of buyer market possible too in the same way (could it ever make sense? who knows?)
- All in all a simple yet flexible modification of PaC, but **MPCC = hard: how about solving it?**

The algorithmic aspects

- MPCC in general \mathcal{NP} -hard, market clearing has to be “quick”
- Routinely done already in practice: Italian PUN, complex offers, ...
- SPaC not fundamentally more difficult than most practical EU markets, MIP-ing complementarity OK because variables nicely bounded
- Besides, when d^r is fixed it \approx boils down to the original clearing problem (an LP if that was, \approx whatever is currently being solved otherwise)
- Trivial approach: (cleverly) finitely sample d^r , return best solution found embarrassingly parallel (MOs can surely buy some large enough server)
- Possibly Benders' style approach (but subproblem may not be convex)
- Typical problem our community loves to deal with, I'd be rather optimistic we can crack it if the interest is there
- But is the interest there? Will it ever be used?

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- My humble take: **in a real market probably not**, but **the energy market is not a real market**, so why not?
- Maybe I'm completely wrong (only a humble optimizer), time will tell

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- Pity because the general idea looks nice and easily applicable
- Anyway, we enjoyed a lot the ride: it's not often you get to step upon the tail of a 50-years old tiger
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